

# **ILP-based Reasoning for Weighted Abduction**

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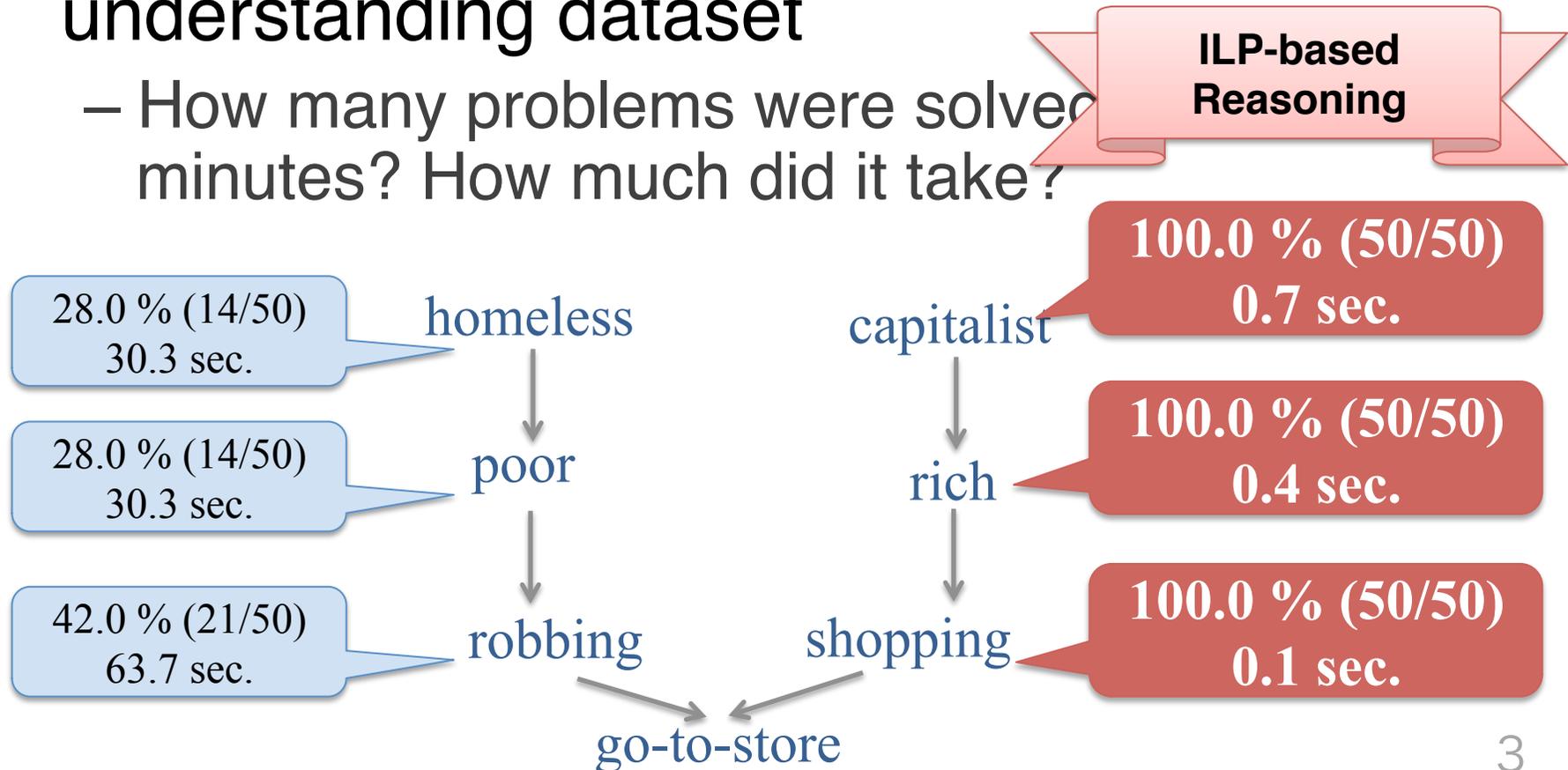
# Introduction

- ◆ **Goal:** Plan recognition from natural language texts
- ◆ Adopt abduction-based framework
  - Hobbs et al. (93)'s Weighted abduction
- ◆ No tools available for large-scale problem

# Scalability Problem

## ◆ Experiments with Mini-TACITUS (Mulkar-Mehta 07) on Ng & Mooney (92)'s story understanding dataset

- How many problems were solved in minutes? How much did it take?



- Introduction
- Weighted Abduction
- ILP-based Reasoning
- Evaluation

# Hobbs+ (93)'s Weighted Abduction

- ◆ Abduction-based framework of natural language understanding
- ◆ “Interpreting sentences is to prove the logical forms of the sentences.”
  - Merging redundancies where possible
  - Making assumptions where necessary
- ◆ Important features
  - Best explanation is selected by assumability costs
  - Evaluating both likelihood and specificity appropriateness of the best explanation

# Abduction

## ◆ Inference to the best explanation

robbing  $\Rightarrow$  go-to-store  
shopping  $\Rightarrow$  go-to-store

“go-to-store” is observed.

shopping      robbing

It's necessary to quantify  
(i) likelihood of  $H$   
(ii) appropriateness of  
specificity of  $H$

## ◆ Formally,

Given

**Background knowledge:**  $B$

**Observations:**  $O$

Find

**Hypothesis:**  $H$  such that

$$H \cup B \models O$$

$$H \cup B \not\models \perp$$

$B, O, H$ : sets of logical formulae

# Scheme of Weighted Abduction

AXIOM:  
assumability weight is assigned

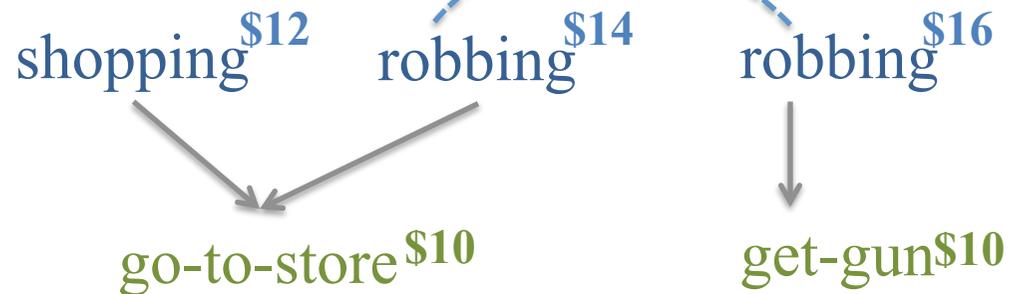
robbing<sup>1.4</sup> ⇒ go-to-store

shopping<sup>1.2</sup> ⇒ go-to-store

robbing<sup>1.6</sup> ⇒ get-gun

BACKCHAINED:  
cost is propagated

UNIFICATION:  
smaller cost is taken



OBSERVATION:  
assumability cost is assigned

**Background knowledge:  $B$**

robbing<sup>1.2</sup> → get-gun

robbing<sup>1.5</sup> → go-to-store

hunting<sup>1.1</sup> → get-gun

shopping<sup>1.4</sup> → go-to-store

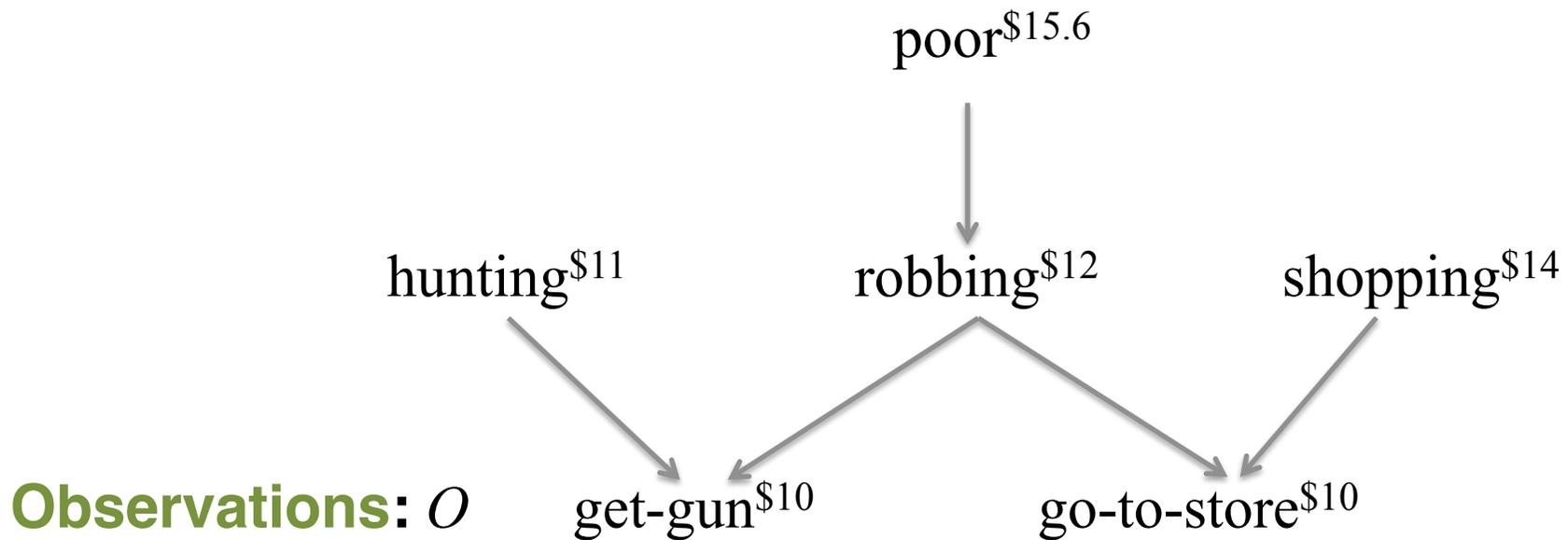
poor<sup>1.3</sup> → robbing

**Hypothesis:  $H$**

{hunting<sup>\$11</sup>, shopping<sup>\$14</sup>}

{robbing<sup>\$12</sup>}

{poor<sup>\$15.6</sup>}



**Background knowledge:  $B$**

- robbing<sup>1.2</sup> → get-gun
- robbing<sup>1.5</sup> → go-to-store
- hunting<sup>1.1</sup> → get-gun
- shopping<sup>1.4</sup> → go-to-store
- poor<sup>1.3</sup> → robbing

**Hypothesis:  $H$**

- {hunting<sup>\$11</sup>, shopping<sup>\$14</sup>}
- {robbing<sup>\$12</sup>}
- {poor<sup>\$15.6</sup>}
- :

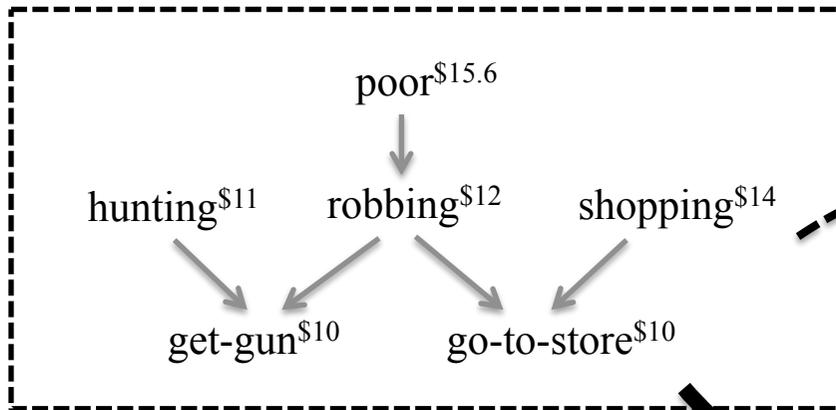
**Implementation Issue:**  
The combinatorial explosion of candidate hypotheses.

Explanation is least-cost explanation  
Most specific hypothesis is selected

**Observations:  $O$**

get-gun<sup>\$10</sup>

go-to-store<sup>\$10</sup>



### Naive approach

$$\begin{aligned}
 H_1 &= \{\text{robbing}^{12}\} \\
 H_2 &= \{\text{poor}^{15.6}\} \\
 H_3 &= \{\text{hunting}^{11}, \text{shopping}^{14}\} \\
 &\vdots \\
 &\arg \min_i C(H_i) \\
 C(H_i) &= \sum_{h \in H_i} c(h)
 \end{aligned}$$

## Our solution: ILP-based Reasoning

### Key ideas:

- ◆ Assign 0-1 ILP variables over all literals potentially included in the best hypothesis for representing candidate hypotheses
- ◆ Cost of hypothesis is represented as the sum of variables
- ◆ There is efficient algorithms to find the optimal assignment of variables

$$\begin{aligned}
 &h_{\text{get-gun}} \quad h_{\text{hunting}} \quad h_{\text{robbing}}, \dots \\
 &r_{\text{get-gun}} \quad r_{\text{hunting}} \quad r_{\text{robbing}}, \dots \\
 &u_{\text{robbing1,robbing2}} \dots
 \end{aligned}$$

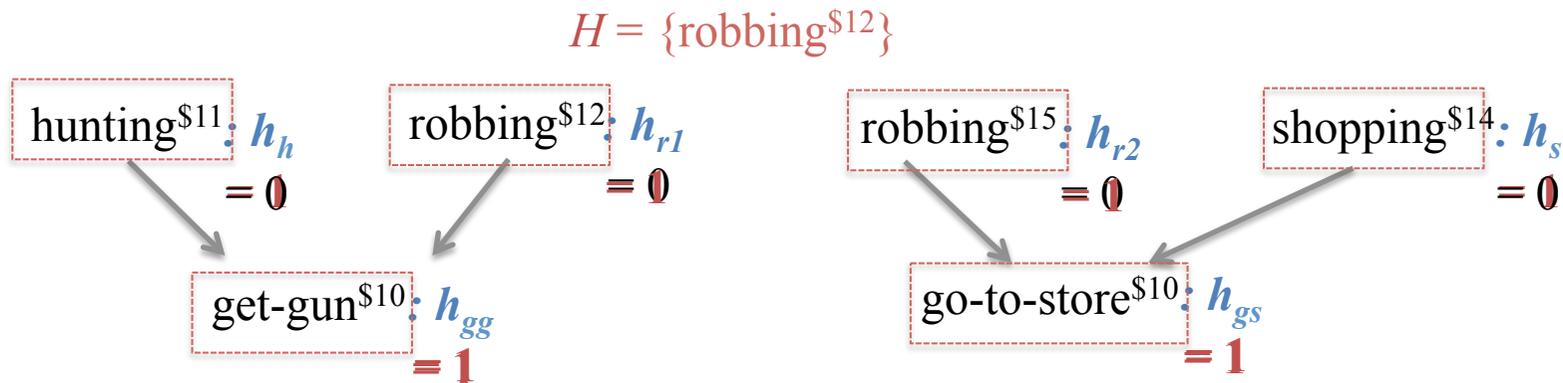
$$\begin{aligned}
 C(H) &= 10 \cdot h_{\text{get-gun}} \\
 &\quad + 11 \cdot h_{\text{hunting}}, \dots
 \end{aligned}$$

$$\arg \min_{h_{\text{get-gun}}, h_{\text{hunting}}, \dots} C(H)$$

# ILP formulation ( $h \rightarrow r \rightarrow u$ )

$$\arg \min_h \sum_{p \in \{p | p \in P, h_p = 1\}} c(p)$$

- ◆  $P$ : set of literals potentially included in hypothesis
- ◆  $h_p$ : 1 if literal  $p$  is included in hypothesis

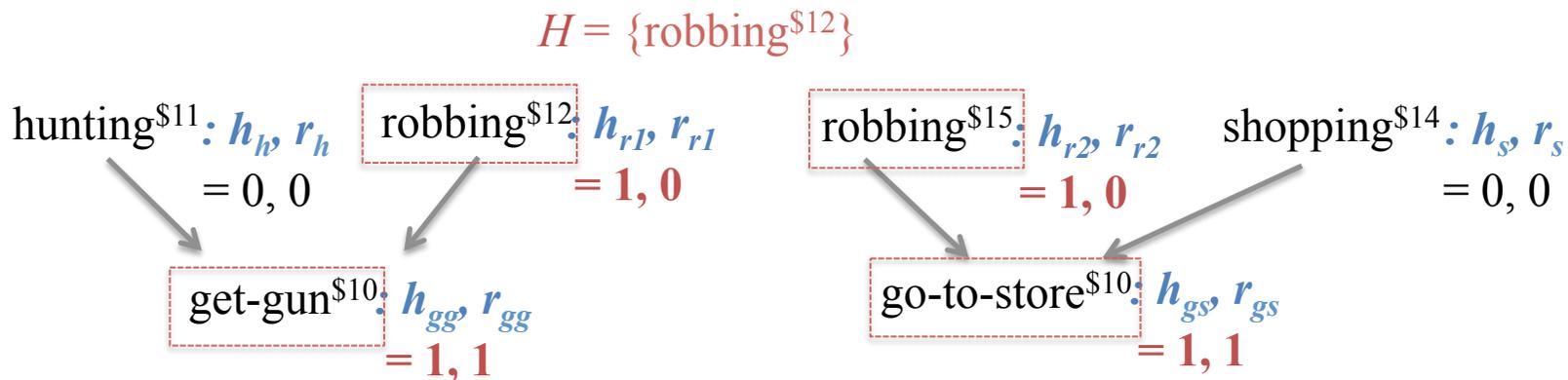


$$P = \{\text{get-gun}, \text{go-to-store}, \text{hunting}, \text{robbing1}, \dots\}$$

# ILP formulation ( $h \rightarrow r \rightarrow u$ )

$$\arg \min_{h,r} \sum_{p \in \{p | p \in P, h_p=1, r_p=0\}} c(p)$$

- ◆  $P$ : set of literals potentially included in hypothesis
- ◆  $h_p$ : 1 if literal  $p$  is included in hypothesis
- ◆  $r_p$ : 1 if literal  $p$  doesn't pay its cost

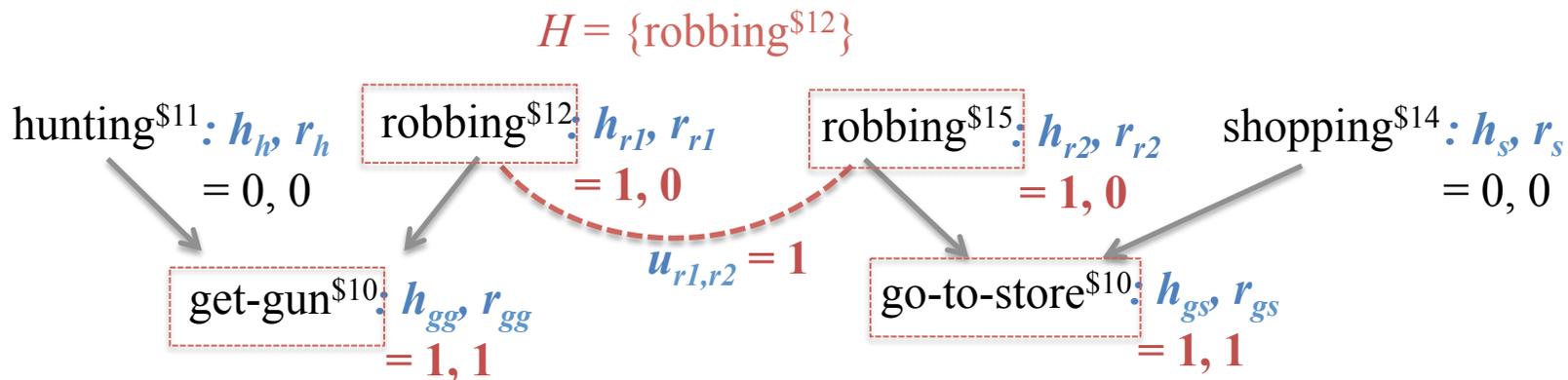


$$P = \{\text{get-gun, go-to-store, hunting, robbing1, ...}\}$$

# ILP formulation ( $h \rightarrow r \rightarrow u$ )

$$\arg \min_{h,r} \sum_{p \in \{p | p \in P, h_p=1, r_p=0\}} c(p)$$

- ◆  $P$ : set of literals potentially included in hypothesis
- ◆  $h_p$ : 1 if literal  $p$  is included in hypothesis
- ◆  $r_p$ : 1 if literal  $p$  doesn't pay its cost
- ◆  $u_{p,q}$ : 1 if literal  $p$  is unified with literal  $q$

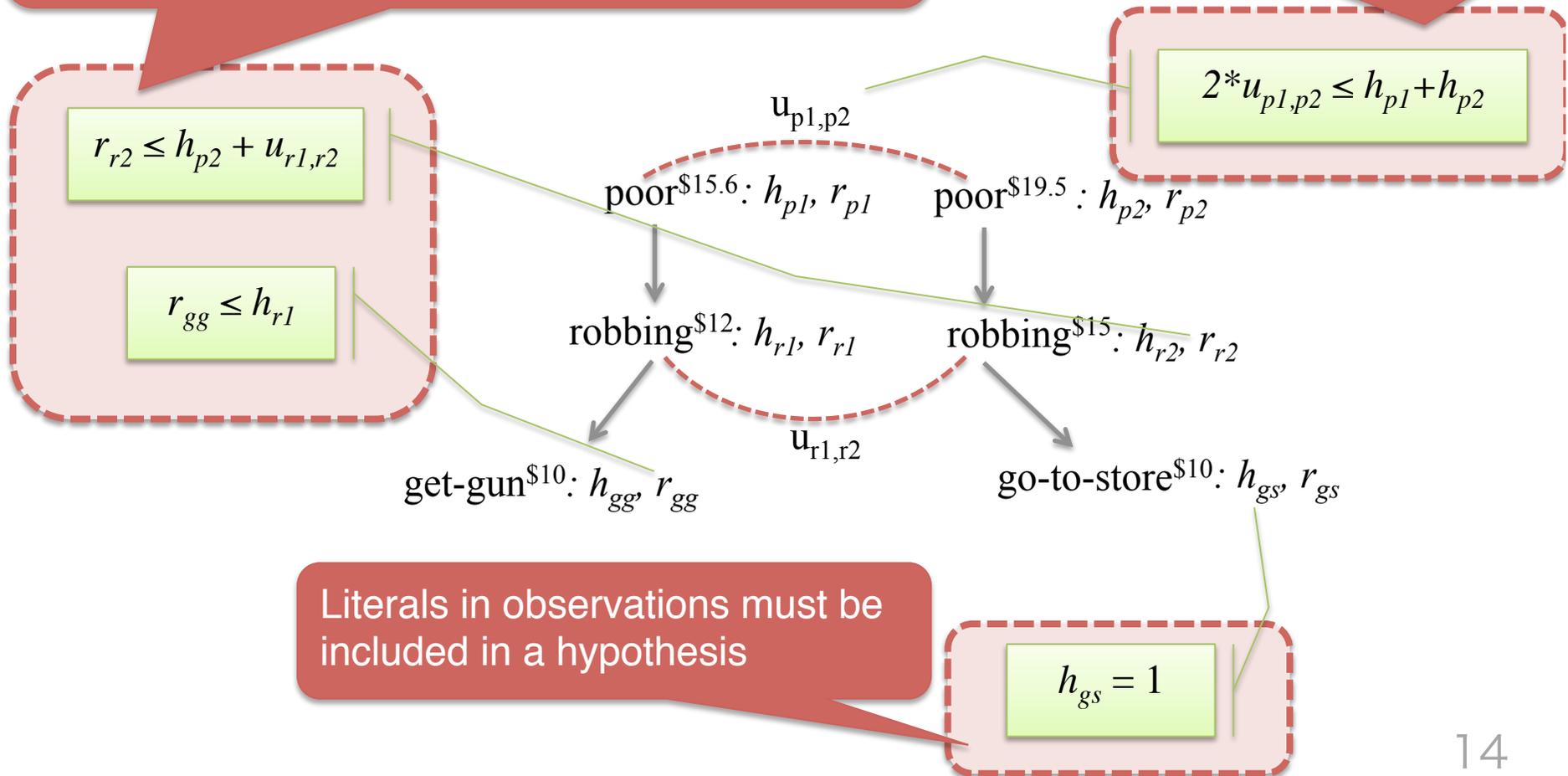


$$P = \{\text{get-gun}, \text{go-to-store}, \text{hunting}, \text{robbing1}, \dots\}$$

# ILP Constraints

Literals do not pay cost ( $r=1$ ) only if they are  
 (i) explained by another literal ( $h=1$ ), or  
 (ii) unified with another literal ( $u=1$ ) of lesser cost

Literals can be unified ( $u=1$ ) only  
 if they are hypothesized ( $h=1$ )

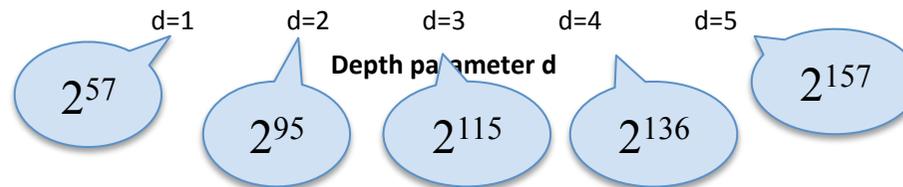


Literals in observations must be  
 included in a hypothesis

# Evaluation

- ◆ How scalable is our approach?
  - Plotted (depth, inference time)
    - The depth limit of back-chaining
    - Inference time averaged for all problems
- ◆ Dataset
  - 50 problems in Ng & Mooney (92)'s story understanding corpus

# Results



- ◆ The increase of inference time is not exponential to the number of candidate hypotheses
  - Indicates the efficiency of our approach!

# Summary

- ◆ Addressed the issue of scalability for abductive reasoning
- ◆ Proposed ILP-based approach to Hobbs et al. (93)'s weighted abduction
- ◆ Results of our experiments showed that:
  - our approach efficiently finds the best explanation
- ◆ Future work
  - Exploring the semantics of weights, costs
  - To handle negation in ILP-based approach

**THANK YOU!**